

# Traction Control of Electric Vehicle based on the Estimation of Road Surface Condition

## - Basic Experimental Results using the Test EV "UOT Electric March" -

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**Abstract-** The most distinct advantage of electric vehicle is in its quick and precise torque generation. We propose two novel traction control techniques of electric vehicle, i.e., the model following control and the optimal slip ratio control. Their effectiveness is demonstrated by using the test vehicle "UOT Electric March".

### I. INTRODUCTION

Recently a lot of electric vehicles (EV) have been developed to solve environment and energy problems caused by the use of internal combustion engine vehicles (ICV). Some of them already have enough performance in practical use. However, they have not yet utilized the most remarkable advantage of EV. Electric motor torque can be controlled much more quickly and precisely than that of internal combustion engine. Adhesion characteristics between tire and road surface are greatly affected by the control of traction motor. This means that the vehicle stability and safety can be improved by motor torque control. If we can use special low drag tires with smaller energy loss, the range of one battery charge will be drastically expanded.

In this paper, we will propose the novel traction control techniques, which can be firstly realized only by utilizing electric motor's quick torque response. They are the model following control and the optimal slip ratio control. By using a newly developed test vehicle "UOT Electric March", we will show some successful experimental results. In order to achieve the best control performance, the estimation method of road surface condition is proposed and its realizability is shown also by real experiments

### II. STATE-OF-THE-ART OF TRACTION CONTROL

Traction control is the control to suppress tire slip when the vehicle is running, for example, on icy road by controlling the traction force and to improve the driving and cornering performances mainly in acceleration.

We should consider two forces acting on the vehicle body, i.e., the driving (longitudinal) and side (lateral) forces. As depicted in Fig.1, these forces depend on the slip ratio

$\lambda$ .  $\lambda$  is defined by eq.(1), where  $V_w$  and  $V$  are the wheel and vehicle speeds.

$$\lambda = (V_w - V) / V_w \quad (1)$$

The side force takes its maximum value when  $\lambda=0$  and becomes smaller for bigger  $\lambda$ . If  $\lambda$  increases by sudden decrease of road friction, the side force gets smaller drastically. This causes serious problems: drift-out in front wheel driven cars, spin in rear wheel driven cars, and drift-out with rotation in four wheel driven cars. Such a loss of cornering force is extremely dangerous. The average traction force is also decreased.

Traction control can be classified into following two steps:

(1) **longitudinal control**, for example, the adhesion improvement to prevent slip. This is done by controlling the traction force, and

(2) **lateral control**, for example, the yaw control to keep the yaw motion to be zero. This is done mainly by controlling the steering angle.

For the lateral control, the steering angle of the front wheels is the absolutely dominant control input. Such a technique is already well developed for ICV and the results can be applied to EV. For this reason, in this paper, we focus our discussion into (1) **longitudinal control**.

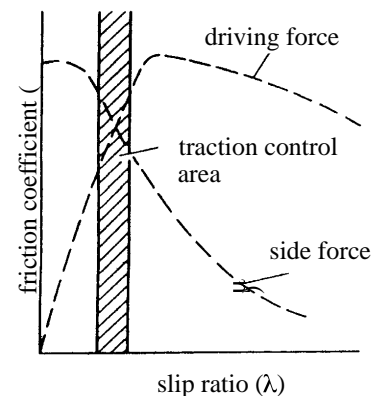


Fig.1. Characteristics of driving and lateral forces

To realize the effective traction control system, we need a sophisticated mechanism quickly to reduce the excessive driving torque. In ICV, this is realized mainly by the following three techniques.

(1) **engine control:** Engine torque itself is suppressed. To reduce air supply is the basic technique, but for quicker response, advanced techniques like fuel-cut and spark timing shift are used together.

(2) **brake control:** Wheel rotation itself can be stopped by braking. This method has quicker response than the engine control. Independent control of left and right tires is effective for  $\mu$ -split braking. Brake control should be used together with the engine control because brake parts often have thermal problem.

(3) **mission control:** Driving torque of the slipping tire is transferred to the non-slipping tire. This technique is effective for  $\mu$ -split road. As the total torque can not be reduced, mission control technique should be applied together with the engine control.

TABLE I summarizes the advantages and disadvantages of these techniques.

TABLE I  
COMPARISON OF TRACTION CONTROLS FOR ICV

	control-lability	response	cost	operation feeling	total
engine control					
brake control				×	
mission control		×			×
engine + mission controls					
engine + brake controls					

### III. ADVANTAGE OF ELECTRIC VEHICLE

Electric Vehicle has great advantages as followings for realization of high performance traction control.

(1) **low cost:** Above mentioned techniques for ICV need additional costly hardware, e.g., throttle and brake actuators. EV does not need anything more. Traction control can be realized only by software. Low cost "basic car" can have high performance traction control.

(2) **quick response:** In ICV, more than 200[ms] are needed to open the throttle actuator. The actual response time is much longer because the mechanical delay is included. In contrast, the response time of electric motor torque is less than 10[ms].

(3) **easy controller design:** In ICV, unknown strong non-linearity lies in the transfer characteristics from the control input (for example, air valve angle to engine, oil pressure of brake system, etc.) to the generated torque. This makes it difficult to construct a mathematical model for controller design. In EV, by applying simple current control, the generated torque is exactly proportional to the torque command.

## IV. MODEL FOLLOWING CONTROL

In this paper, we propose two control strategies: one is the **model following control (MFC)**, and another is the **optimal slip ratio control**. MFC is the starting point of our research project of "Control of Electric Vehicle" and its basic feasibility is demonstrated here by real experiment.

### A. Principle of MFC

Fig.2 shows the block diagram of the model following control.  $I_{com}$  is the current command proportional to the acceleration pedal angle.  $\omega$  is the rotational speed of the driving shaft.  $\omega$  increases drastically when the tire slips. Vehicle dynamics including tire characteristics and road surface friction are very complicated, but if we introduce the slip ratio  $\lambda$ , the vehicle body can be seen as one inertia system having the equivalent inertia moment of

$$J = J_w + Mr^2(1-\lambda) \quad (2)$$

Here,  $J_w$ ,  $M$  and  $r$  are the shaft inertia moment, vehicle weight and tire radius. Eq.(2) means that, when slip occurs, the vehicle seems lighter. Therefore, we use the following inertia moment with  $\lambda=0$  in the reference model.

$$J_{model} = J_w + Mr^2 \quad (3)$$

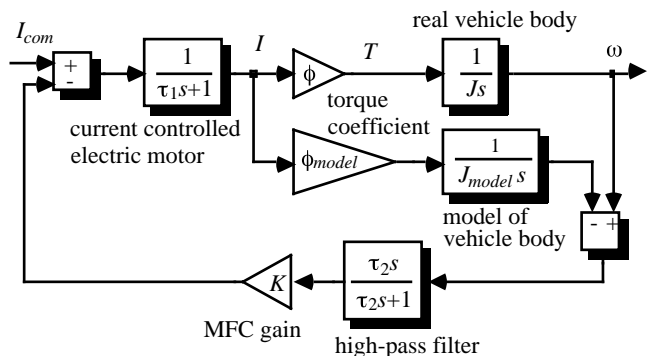


Fig.2. Block diagram of MFC

When there is no slip, actual  $J$  is almost equal to  $J_{model}$ . Any signal is not generated from MFC controller. If the tire slips, the actual wheel speed  $\omega$  increases immediately. The model wheel speed does not increase. By feeding back the speed difference to the motor current command, the

actual motor torque is reduced quickly and it induces re-adhesion.

This control function is needed only in relatively higher frequency region, we used a high pass filter on the feedback pass. In actual implementation, two high pass filters are inserted before taking the difference between actual and model speeds to avoid the offset problem of integrator.

### B. Experimental Result of MFC

Fig.3 shows the slip experiment using UOT Electric March. We used iron plates as slippery road surface. Water is scattered to reduce the friction coefficient. The vehicle is accelerated by the constant current command of 300[A]. The feedback gain  $K$  in Fig.2 is 30. The front wheels are on the slippery area between  $t=1.25[s]$  and  $1.7[s]$ .

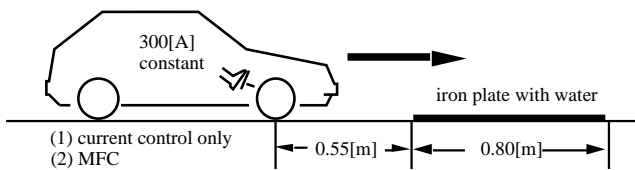


Fig.3. Slip experiment

Experimental results are given in Fig.4. We can see that MFC can reduce the motor current effectively when the vehicle goes onto the slippery area, and then the slip ratio is kept much lower comparing to the current control only. Some vibration seen in the current waveform in Fig.4(a) should be suppressed in the future.

## V. OPTIMAL SLIP RATIO CONTROL

The model following control is a very rough approach although it has been shown that the motor control is really effective for adhesion improvement. If we want more exactly to regulate the slip ratio within the desired range, more precise approach is needed. Fig.5 shows the idea of the optimal slip ratio control developed from this viewpoint. When the optimal slip ratio is decided by the road condition estimator, the slip ratio controller receives the command and realizes it.

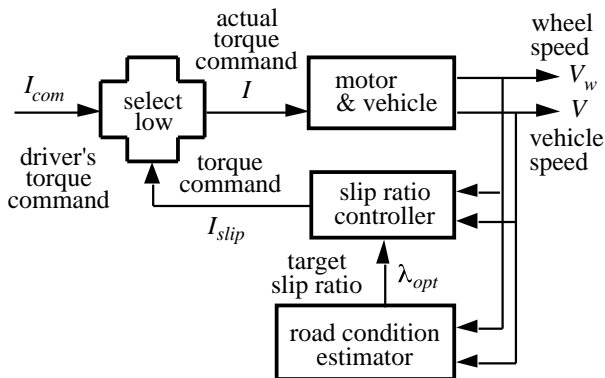
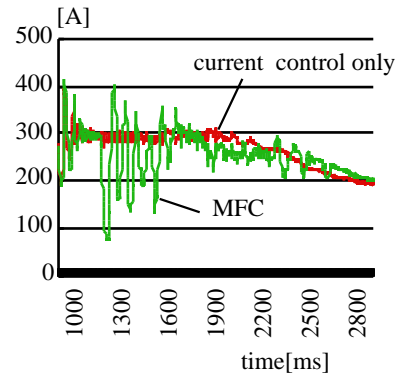
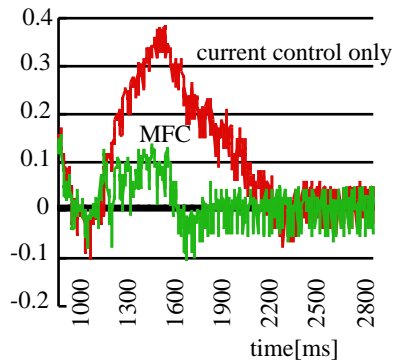


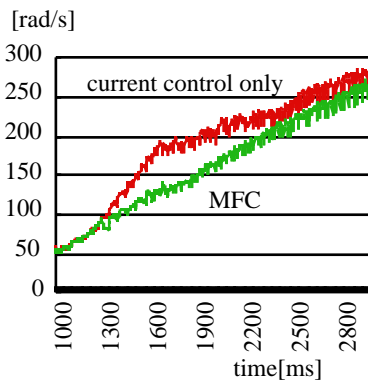
Fig.5. Block diagram of the optimal slip ratio controller



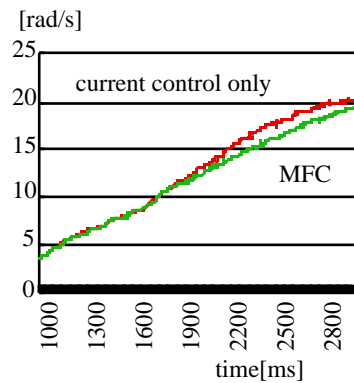
(a) motor current



(b) slip ratio



(c) wheel speed



(d) vehicle speed

Fig.4. Experimental results of MFC

### A. Vehicle Model

We assume that the two motor torques and friction forces are same in left and right, and that the rolling and air frictions are small enough. In Fig.6, the kinematic equations of the wheel and vehicle take the forms of

$$(F_m - F_d) \frac{1}{M_w s} = V_w \quad (4)$$

and

$$F_d \frac{1}{M s} = V \quad (5)$$

where,

- $F_m$  : motor torque (force equivalent)
- $F_d$  : friction force
- $M_w$  : wheel inertia (mass equivalent)
- $M$  : vehicle weight

The friction force between the road and wheel is given by

$$F_d = N \mu(\lambda) \quad (6)$$

where  $N$  is the vertical force given by  $N = Mg$ .

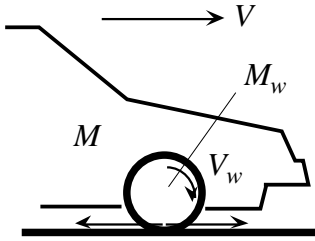


Fig.6. Vehicle model.

From eq.(1), the following perturbation system is derived.

$$\begin{aligned} \Delta \lambda &= \frac{\partial \lambda}{\partial V} \Delta V + \frac{\partial \lambda}{\partial V_w} \Delta V_w \\ &= -\frac{1}{V_{w0}} \Delta V + \frac{V_0}{V_{w0}^2} \Delta V_w \end{aligned} \quad (7)$$

where  $V_{w0}$  and  $V_0$  are the wheel and vehicle speeds at the operational point. The friction force is represented using  $a$ , the gradient of  $\mu-\lambda$  curve, as

$$\Delta \mu = a \Delta \lambda \quad (8)$$

By combining eqs.(7) and (8) with the perturbed forms of eqs. (4) and (5), the transfer function from the motor torque to the slip ratio is finally given by

$$\frac{\Delta \lambda}{\Delta F_m} = \frac{1}{Na} \frac{M(1-\lambda)}{M_w + M(1-\lambda)} \frac{1}{1+\tau s} \quad (9)$$

where the time constant  $\tau$  is given by eq.(10) which is proportional to the wheel speed  $V_{w0}$ .

$$\tau = \frac{1}{Na} \frac{MM_w V_{w0}}{M_w + M(1-\lambda)} \quad (10)$$

The typical value of  $\tau$  in our experimental vehicle is 150 ~ 200[ms] when  $a=1$  and the vehicle speed is around 10[km/h]. Note that  $a$  can be negative in the right-hand side of the peak point of  $\mu-\lambda$  curve.

### B. Design of Slip Ratio Controller

We used a simple P&I controller with a variable gain as the slip ratio controller given by eq.(11). Its nominator compensates for the pole of eq.(9). The integral gain is constant and the proportional gain is proportional to the vehicle speed.

$$K \frac{1+\tau s}{s} \quad (11)$$

Finally, the transfer function from the slip ratio command to the actual slip ratio becomes

$$\frac{\Delta \lambda}{\Delta \lambda^*} = \frac{1}{1 + Na \frac{M_w + M(1-\lambda)}{M(1-\lambda)} \frac{1}{K} s} \quad (12)$$

If  $\lambda \ll 1$ , this is a simple first order delay characteristics with a time constant which can be adjusted by  $K$ . Here, we put this response time 50 ~ 100[ms].

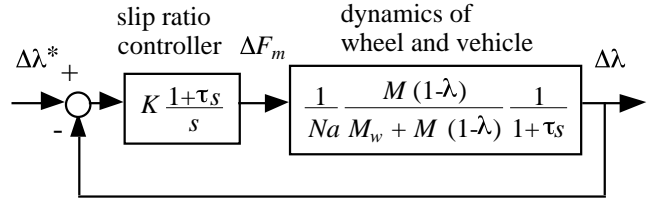


Fig.7. Slip ratio controller

Fig.8 shows the nominal slip ratio used in the slip ratio controller. We defined it by  $a=1$ . The point of  $a=1$  is located just in left side of the peak and is stable. Both of the longitudinal and lateral forces are kept still high.

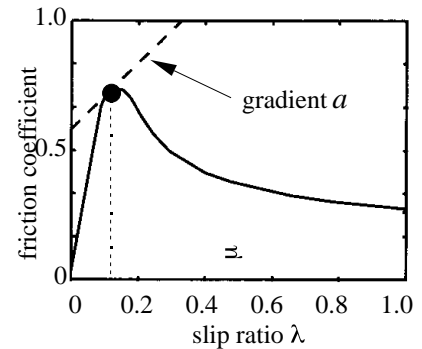


Fig.8. Nominal slip ratio is given by  $a=1$ .

### C. Robustness to Parameter Variation

Because the actual system parameters change widely, we should investigate the robustness of the slip ratio controller. Fig.9 draws the root locus to the continuous change of  $K$  and  $a$ .

From the figure, we can see that the roots move to the left half plane when the controller gain  $K$  increases. It is interesting that this controller stabilizes the system even when actual  $a$  is negative, although the roots move to unstable region.

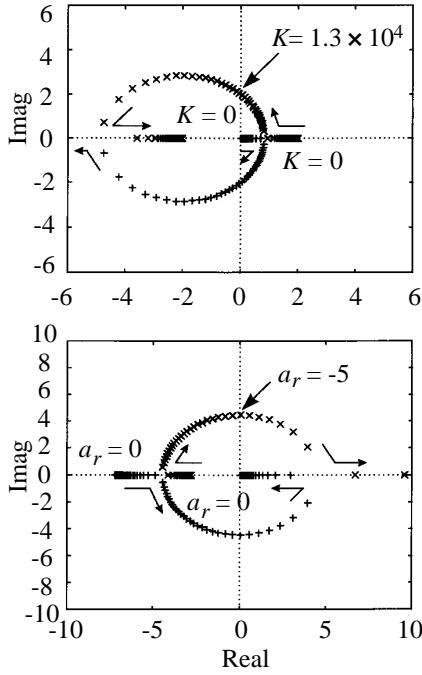


Fig.9. Root locus against parameter variation

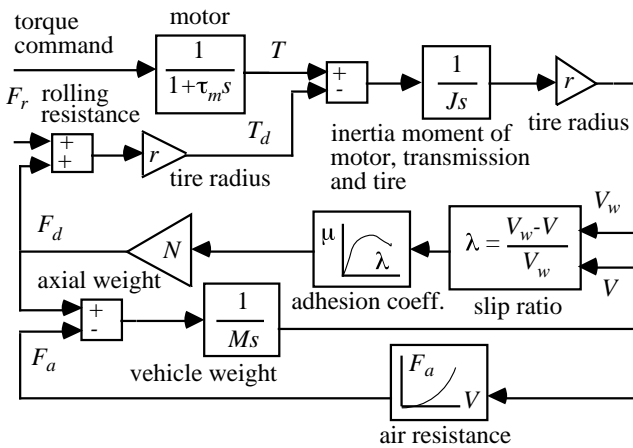


Fig.10 Vehicle model used in the simulation

### D. Simulation of Slip Ratio Control

Fig.10 shows the vehicle model we used in the simulation.  $T$  represents the motor torque and  $r$  the total gear ratio of the drive train.  $F_d$  represents the summation of traction

force transferred to the contact point of tire and road surface. It is the product of traction coefficient  $\mu$  and  $N=Mg$ , the vertical load on the contact point.  $\mu$  is defined as a function of  $\lambda$  (slip), which is given by the measured curve shown in Fig.11.

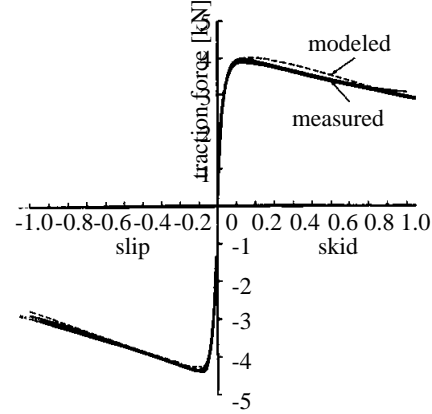


Fig.11.  $\mu$ - $\lambda$  characteristics used in the simulation

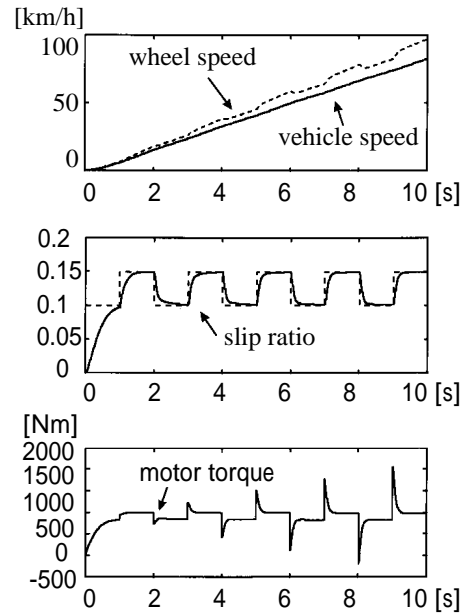


Fig.12 Simulation of the slip ratio control

Fig.12 is the simulation result. The response time of the slip ratio controller is set to be 100[ms]. We can see good response characteristics.

### E. Experimental Results of Slip Ratio Control

Fig.13 shows the experimental results of the slip ratio control using the laboratory-made experimental electric vehicle "UOT Electric March". Here the response time is 50[ms] and the target slip ratio is 0.1 in Fig.13(a) and is changed stepwise from 0.3 to 0.1 in Fig.13(b).

Basically we can see fairly good performances but there are some problems. First, the actual value of  $a$  was much smaller than the nominal value: 1. This made the response

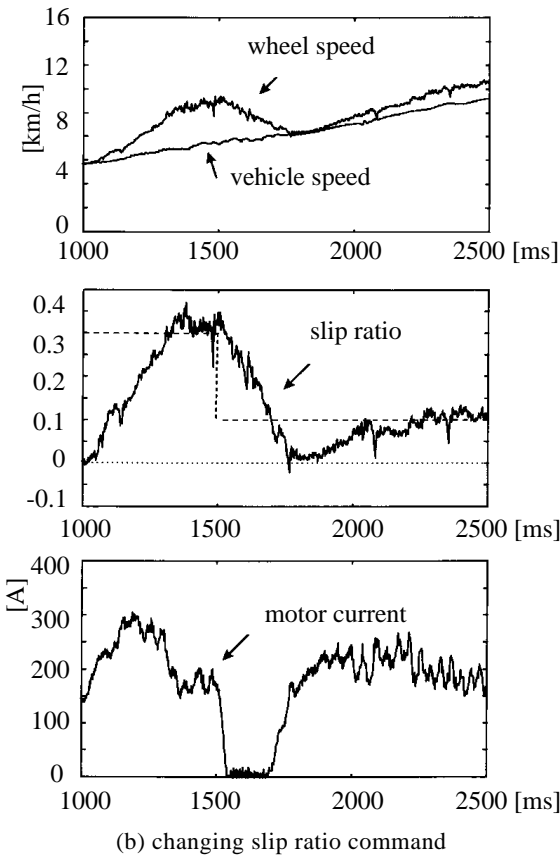
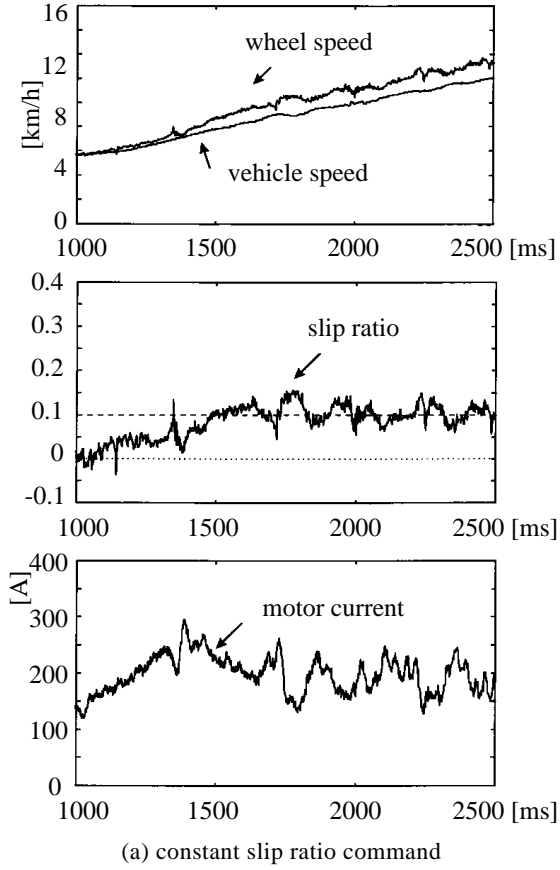


Fig.13. Experimental results of the slip ratio control

time longer than the designed value. Next, in Fig.13(b), we see an undershoot to the slip ratio command of 0.1. This is because the motor controller we used is just an 1-quadrant chopper, who can not absorb the motor current.

## VI. ESTIMATION OF ROAD CONDITION

In the previous chapter, we showed effective slip ratio control. Next problem is how to give the optimal slip ratio to the slip ratio controller.

We showed the relation between the slip ratio  $\lambda$  and the friction coefficient  $\mu$  in Figs.1 and 11, but it varies very widely according to road surface condition as shown in Fig.14. It is clear that the slip ratio where the friction force takes its maximum value vary according to road condition. This means that road condition should be estimated relatively quickly for commanding the optimal slip ratio to the slip ratio control.

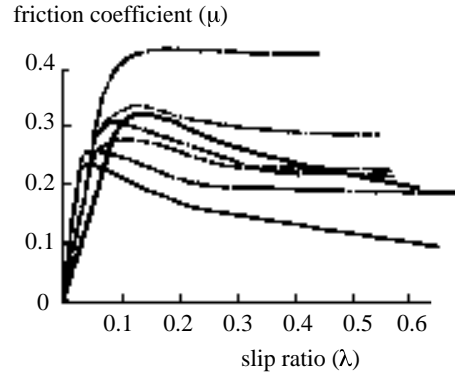


Fig.14. Various Road Condition.  
(Actual explanation of each curves is omitted.)

To know the road surface condition, we should estimate the friction coefficient. If we can measure the vehicle speed directly by using non-driven wheel, the friction coefficient  $\mu$  can be obtained by eq.(13) based on eqs.(3) and (4).

$$\mu = \frac{M}{N} \frac{dV}{dt} \quad (13)$$

When the vehicle speed can not be measured directly, we can estimate  $\mu$  based on eq.(14).

$$\mu = \frac{1}{N} \left( F_m - M_w \frac{dV_w}{dt} \right) \quad (14)$$

In our case, we can use both of these two methods. Fig.15 shows the estimation result of  $\mu$ - $\lambda$  curve of dry asphalt road when no slip control is active. At the point around  $\lambda=0.08$ , the gradient  $a$  of  $\mu$ - $\lambda$  curve is about 1.

Fig.16 shows the estimation results on wet iron surface under the slip ratio control proposed in the previous chapter. Here, the optimal slip ratio is smaller than 0.05.

It is also noticed that, in our experiment shown in Fig.13(a), the actual gradient of  $\mu$ - $\lambda$  curve at  $\lambda=0.1$  was almost -1. We can see that the slip ratio controller is effective even when the operation point is unstable, but, in this case, we should have commanded a lower slip ratio.

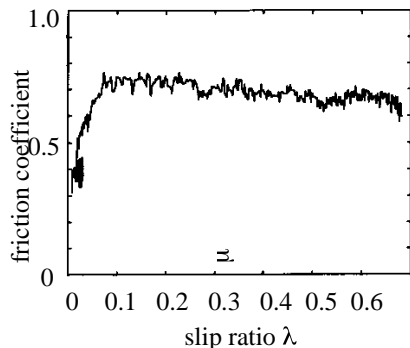


Fig.15. Estimation result of  $\mu$ - $\lambda$  curve of dry asphalt road

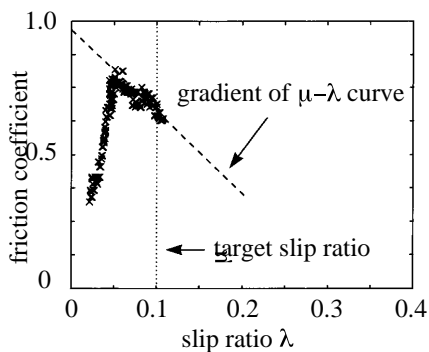


Fig.16. Estimation result of  $\mu$ - $\lambda$  curve of wet iron plate under the slip ratio control

## VII. CONCLUSION

We are proposing a new field of "Motion Control of Electric Vehicle". EV is a very interesting object combining electrical and mechanical engineering fields from the view point of motion control. As an example, we proposed advanced adhesion control utilizing quick and precise torque response of electric motor.

We proposed the Model Following Control and the Optimal Slip Ratio Control. We confirmed that MFC can reduce its torque quickly when the motor speed is suddenly increased by tire slip. Next, we showed that the optimal slip ratio control has more advanced performance. Such kinds of quick controls are firstly realized only in electric vehicles. It is clearly shown that relatively precise control theory can work well in actual experiments.

Advanced adhesion control is helpful for lateral control like yaw disturbance attenuation. This is because the proposed optimal slip ratio control keeps the tire slip within the small region where both of the longitudinal and lateral adhesion coefficients are still high enough.

## ACKNOWLEDGEMENT

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## APPENDIX

### Configuration of UOT Electric March

We developed a real test electric vehicle "UOT Electric March (Todai Sangatsu Go)" seen in Fig.A-1. It is a so-called convert car, whose IC engine is replaced by an electric motor.

The front two wheels are driven by a 19[kW] series-wound DC motor through a 5 speed manual transmission and a differential gear. The 1-quadrant DC chopper supplies power to the motor. Its current limit is 400[A] and can produce maximum torque over 100[Nm], which is enough to perform the slip experiment. Current and speed sensors are also implemented. To detect the vehicle speed, a speed sensor is implemented in the rear wheel.

TABLE A-I  
SPECIFICATION OF UOT ELECTRIC MARCH

<b>Conversion Base</b>	Nissan March (Micra)
size	3785 × 1560 × 1395[mm]
weight	900[kg](batteries included)
<b>Motor</b>	Advanced D.C. Motors, Inc.
type	DC series wound
rated power (@120V)	19[kW](1hr.), 32[kW](5min.)
size/weight	φ 232, length 397[mm], 65[kg]
<b>Controller</b>	Curtis Instruments, Inc.
type	MOSFET PWM Chopper
operating frequency	15[kHz]
rated voltage/current	120[V]/400[A]
<b>Battery</b>	Japan Storage Battery Co.,Ltd. GTX-130E41L
type	lead acid
voltage/capacity	72[V]/92[Ah](5hr)
weight	27.5[kg] × 6
<b>CPU</b>	PC9801NS/T (386SL, 20MHz)
weight	3.2[kg]
A/D and D/A converters	12bit, 8ch / 12bit, 2ch

Fig.A-2 shows the control system of the vehicle and TABLE A-I gives its specification. We use a note-type personal computer to realize the torque control. It not only executes the control algorithm and puts out the voltage command to the chopper, but also reads, shows and records the sensor data. As the control algorithm is written by software (C-language), we can easily investigate various

control strategies.

Fig.A-3 shows the basic experimental results of the current controller.



Fig.A-1 UOT Electric March (Todai Sangatsu Go)

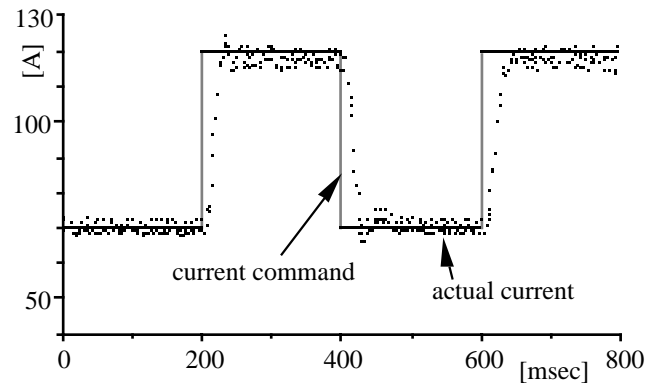


Fig.A-3. Basic experiment on the current response

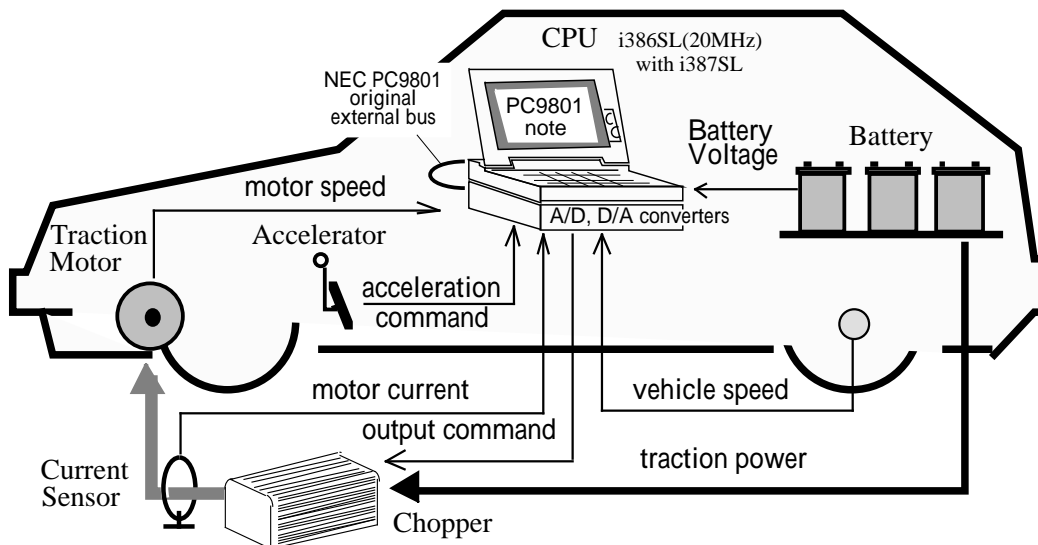


Fig.A-2 Configuration of UOT Electric March